

The Design of NaBL2: From Theory (of Name Resolution) to Practice

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Motivation



Package Explorer

- pom.xml
- org.metaborg.lang.tiger.eclipse
- org.metaborg.lang.tiger.eclipse.featur
- org.metaborg.lang.tiger.eclipse.site
- > org.metaborg.lang.tiger.example [m]
 - JRE System Library [JavaSE-1.8]
 - Maven Dependencies
 - appel
 - > examples
 - arith.aterm
 - arith.tig
 - fac-error.pp.tig
 - > fac-error.tig
 - fac-formatted.tig
 - fac.aterm
 - fac.des.tig
 - fac.pp.tig
 - > fac.tig
 - fact-anf.aterm
 - fact-anf.tig
 - fact-anf2.tig
 - for.aterm
 - for.des.aterm
 - for.des.tig
 - > for.tig
 - incomplete.tig
 - let-binding.tig
 - list-type.tig
 - nested.tig
 - point.aterm
 - point.pp.tig
 - point.tig
 - queens.aterm
 - queens.pp.tig
 - > queens.tig

```

1 /* A program to solve the 8-queens problem */
2
3 let
4   var N := 8
5
6   type intArray = array of int
7
8   var row := intArray [ N ] of 0
9   var col := intArray [ N ] of 0
10  var diag1 := intArray [N+N-1] of 0
11  var diag2 := intArray [N+N-1] of 0
12
13
14  function printboard() =
15    (for i := 0 to N-1
16     do (for j := 0 to N-1
17        do print(if col[i]=j then " 0" else " .");
18           print("\n"));
19       print("\n"))
20
21  function try(c:int) =
22  (
23    if c=N
24    then printboard()
25    else for r := 0 to N-1
26         do if row[r]=0 & diag1[r+c]=0 & diag2[r+7-c]=0
27            then (row[r]:=1; diag1[r+c]:=1; diag2[r+7-c]:=1;
28                 col[c]:=r;
29                 try(c+1);
30                 row[r]:=0; diag1[r+c]:=0; diag2[r+7-c]:=0)
31  )
32 end

```

Console

<terminated> Tiger [Java Application]

```

. . . . . 0 . .
. . . . . 0
. 0 . . . . .
. . . . . 0 . .
. . 0 . . . . .
0 . . . . .
. . . . . 0 .
. . . 0 . . . .
. . . . . 0 . .
. . . . . 0 .
. . . 0 . . . .
. . . . . 0
. . . . . 0
0 . . . . .
. . 0 . . . . .
. . . . . 0 .
. 0 . . . . .
. . . . . 0 .
. . . . . 0 .

```

UnitV()

Language Workbench

**Syntax
Definition**

+

**Static
Semantics**



**Programming
Environment**

+

**Dynamic
Semantics**

Spoofax Language Workbench

```
Functions.sdf3
1 module Functions
2
3 imports Identifiers
4 imports Types
5
6 context-free syntax
7
8 Dec.FunDecs = <<{FunDec "\n"}+>> {longest-m
9
10 FunDec.ProcDec = <
11   function <Id>(<{FArg ", "}*>) =
12     <Exp>
13 >
14
15 FunDec.FunDec = <
16   function <Id>(<{FArg ", "}*>) : <Type> =
17     <Exp>
18 >
19
20 FArg.FArg = <<Id> : <Type>>
21
22 Exp.Call = <<Id>(<{Exp ", "}*>)>

functions.nabl2
33 //
34 [[ t ^ (s_outer) : ty ]],
35 Var{f} <- s,
36 Var{f} : FUN(tys, ty) !,
37 [[ e ^ (s_fun) : ty_body ]],
38 ty = ty_body | error $[return type does not
39
40 Args[[ args ^ (s_fun, s_outer) : tys ]] :=
41   new s_fun,
42   s_fun -P-> s,
43   distinct/name D(s_fun) | error $[duplicate
44   MapTs2[[ args ^ (s_fun, s_outer) : tys ]].
45
46 [[ FArg(x, t) ^ (s_fun, s_outer) : ty ]] :=
47   Var{x} <- s_fun,
48   Var{x} : ty !,
49   [[ t ^ (s_outer) : ty ]].
50
51 rules // function calls
52
53 [[ Call(f, exps) ^ (s) : ty ]] :=
54   Var{f} -> s,
55   Var{f} |-> d | error $[Function [f] not dec
56   d : FUN(tys, ty) | error $[Function expecte
57   MapSTs[[ exps ^ (s) : tys ]].
58

functions.ds
23 FunDecs(fds) --> E
24 where
25   funEnv(fds) --> E;
26   E |- evalFuns(fds) --> _
27
28 E |- funEnv([]) --> E
29
30 funEnv([FunDec(f, _, _, _) | fds]) --> E
31 where
32   E bindVar(f, UndefV()) |- funEnv(fds) --> I
33
34 E |- evalFuns([]) --> E
35
36 E |- evalFuns([FunDec(f, args, _, e) | fds])
37 where
38   writeVar(f, ClosureV(args, e, E)) --> _
39
40 rules // function call
41
42 Call(f, args) --> v
43 where
44   readVar(f) --> ClosureV(params, e, E);
45   evalArgs(params, args) --> E';
46   E {E', E} |- e --> v
47
48 evalArgs([], []) --> []

fac.tig
1 let function fact(n : int) : int =
2   if n < 1 then 1 else (n * fact(n - 1))
3 in fact(10)
4 end

fac.aterm
1 Mod(
2   Let(
3     [ FunDecs(
4       [ FunDec(
5         "fact"
6         , [FArg("n", Tid("int"))]
7         , Tid("int")
8         , If(
9           Lt(Var("n"), Int("1"))
10          , Int("1")
11          , Seq(
12            [ Times(
13              Var("n")
14            ]
15          )
16        )
17      ]
18    )
19  )
20 )

Console
<terminated> Tiger [Java Application] /Library/Java/JavaVirtualMachines/
IntV(3628800)
```

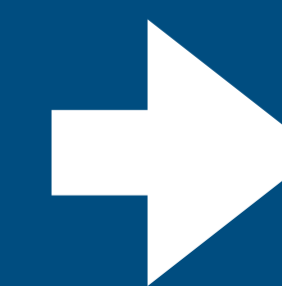
SDF3: Syntax
Definition

+

NaBL2: Static
Semantics

+

DynSem: Dynamic
Semantics



Programming
Environment

Separation of Concerns

Representation

- Standardized representation for <aspect> of programs
- Independent of specific object language

Specification Formalism

- Language-specific declarative rules
- Abstract from implementation concerns

Language-Independent Interpretation

- Formalism interpreted by language-independent algorithm
- Multiple interpretations for different purposes
- Reuse between implementations of different languages

Separation of Concerns in Syntax Definition

Representation: (Abstract Syntax) Trees

- Standardized representation for structure of programs
- Basis for syntactic and semantic operations

Formalism: Syntax Definition

- Productions + Constructors + Templates + Disambiguation
- Language-specific rules: structure of each language construct

Language-Independent Interpretation

- Well-formedness of abstract syntax trees
 - provides declarative correctness criterion for parsing
- Parsing algorithm
 - No need to understand parsing algorithm
 - Debugging in terms of representation
- Formatting based on layout hints in grammar
- Syntactic completion



A meta-language for talking about syntax

Separation of Concerns in Name Binding

Representation

- To conduct and represent the results of name resolution

Declarative Rules

- To define name binding rules of a language

Language-Independent Tooling

- Name resolution
- Code completion
- Refactoring
- ...

NaBL: Name Binding Language

Konat, Kats, Wachsmuth, Visser. Declarative Name
Binding and Scope Rules. SLE 2012

Interaction with Type System (I)

FieldAccess(e, f):
refers to Field f in c
where e has type ClassType(c)

```
class C {  
    int i;  
}  
  
class D {  
    C c;  
    int i;  
    void init() {  
        i = c.i;  
    }  
}
```

Name Binding

defines

refers

namespaces

scopes

imports

class
partial class

type
inheritance

namespace
using

method
field
variable
parameter
block

Theory: Scope Graphs

Néron, Tolmach, Visser, Wachsmuth. A
Theory of Name Resolution. ESOP 2015

Separation of Concerns in Name Binding

Representation

- **Scope Graphs**

Declarative Rules

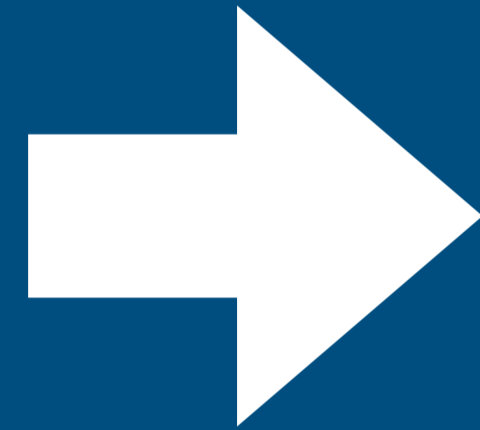
- To define name binding rules of a language

Language-Independent Tooling

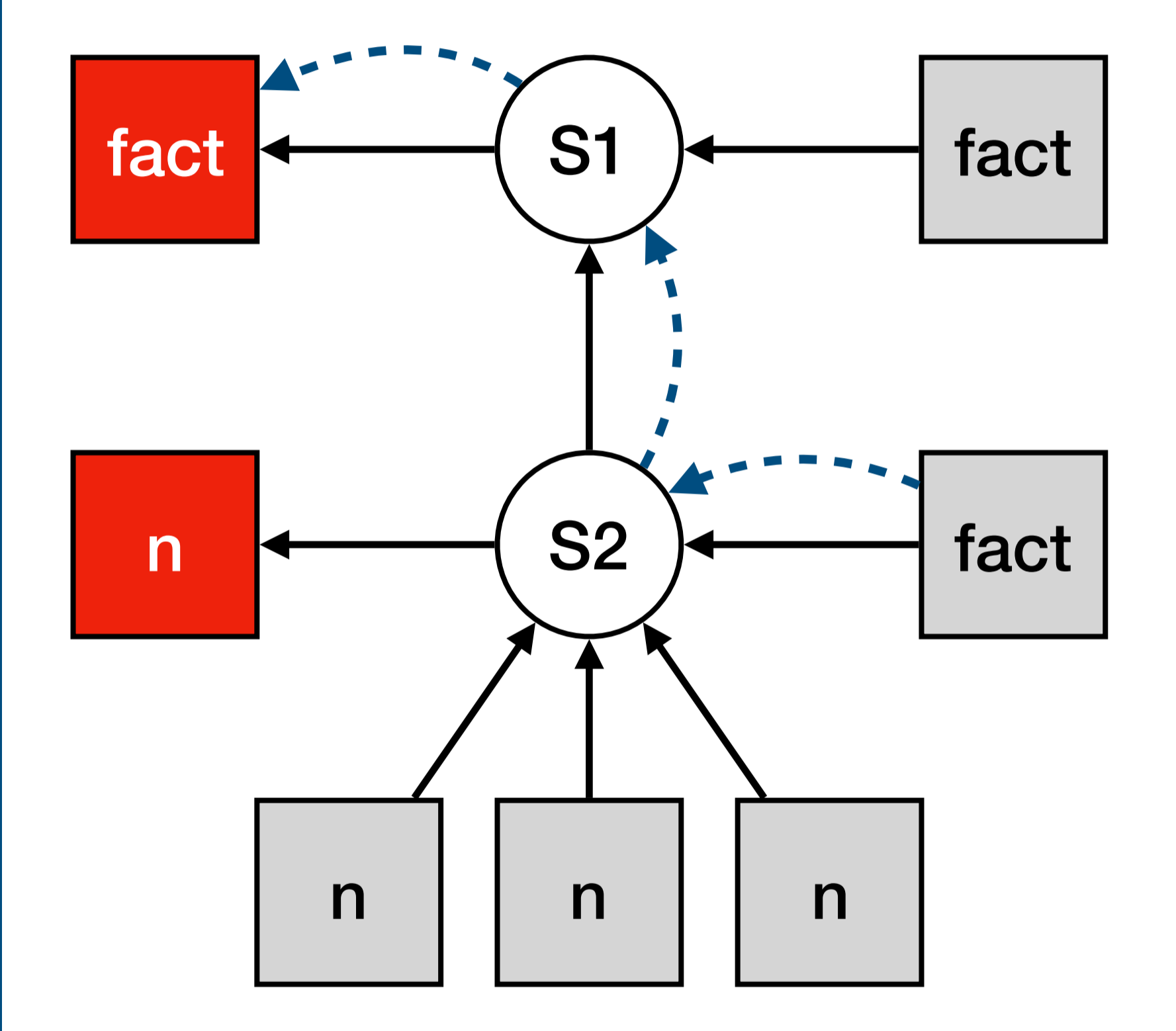
- Name resolution
- Code completion
- Refactoring
- ...

Program

```
let function fact(n : int) : int =  
  if n < 1 then  
    1  
  else  
    n * fact(n - 1)  
  in  
  fact(10)  
end
```

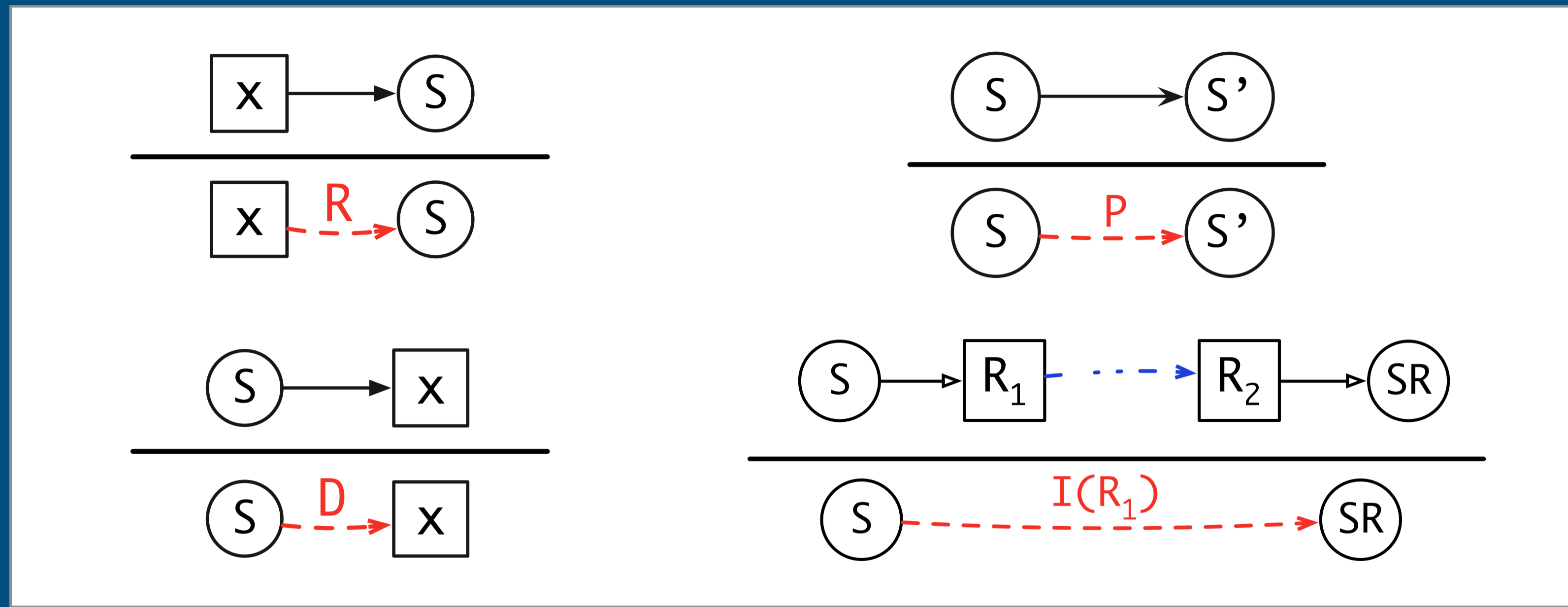


Scope Graph



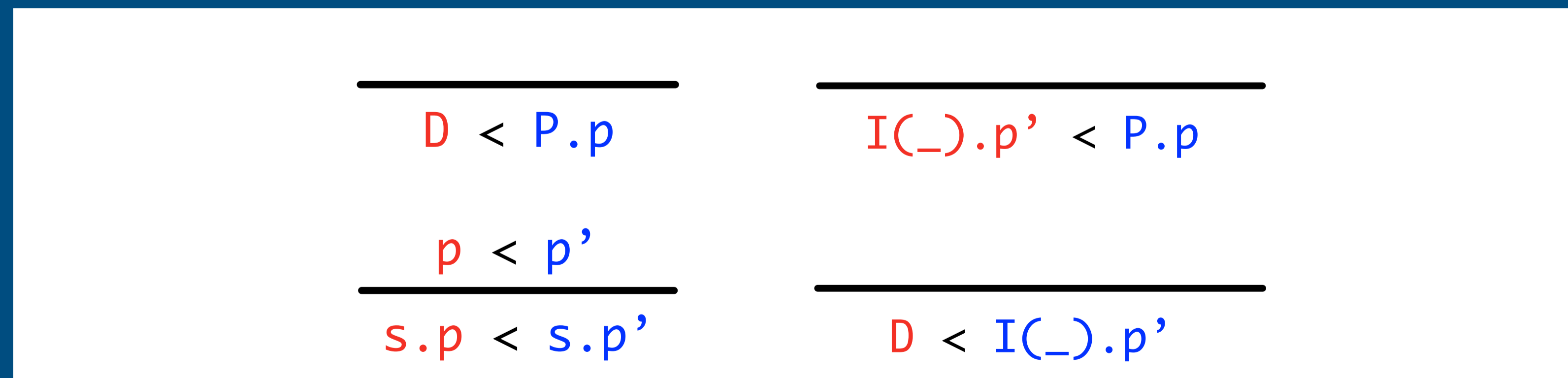
Name Resolution

A Calculus for Name Resolution



Reachability

Well formed path: $R.P^*.I(_)*.D$



Visibility

Visibility Policies

Lexical scope

$$\mathcal{L} := \{\mathbf{P}\} \quad \mathcal{E} := \mathbf{P}^* \quad \mathbf{D} < \mathbf{P}$$

Non-transitive imports

$$\mathcal{L} := \{\mathbf{P}, \mathbf{I}\} \quad \mathcal{E} := \mathbf{P}^* \cdot \mathbf{I}^? \quad \mathbf{D} < \mathbf{P}, \quad \mathbf{D} < \mathbf{I}, \quad \mathbf{I} < \mathbf{P}$$

Transitive imports

$$\mathcal{L} := \{\mathbf{P}, \mathbf{TI}\} \quad \mathcal{E} := \mathbf{P}^* \cdot \mathbf{TI}^* \quad \mathbf{D} < \mathbf{P}, \quad \mathbf{D} < \mathbf{TI}, \quad \mathbf{TI} < \mathbf{P}$$

Transitive Includes

$$\mathcal{L} := \{\mathbf{P}, \mathbf{Inc}\} \quad \mathcal{E} := \mathbf{P}^* \cdot \mathbf{Inc}^* \quad \mathbf{D} < \mathbf{P}, \quad \mathbf{Inc} < \mathbf{P}$$

Transitive includes and imports, and non-transitive imports

$$\mathcal{L} := \{\mathbf{P}, \mathbf{Inc}, \mathbf{TI}, \mathbf{I}\} \quad \mathcal{E} := \mathbf{P}^* \cdot (\mathbf{Inc} \mid \mathbf{TI})^* \cdot \mathbf{I}^?$$

$$\mathbf{D} < \mathbf{P}, \quad \mathbf{D} < \mathbf{TI}, \quad \mathbf{TI} < \mathbf{P}, \quad \mathbf{Inc} < \mathbf{P}, \quad \mathbf{D} < \mathbf{I}, \quad \mathbf{I} < \mathbf{P},$$

Separation of Concerns in Name Binding

Representation

- **Scope Graphs**

Declarative Rules

- To define name binding rules of a language

Language-Independent Tooling

- Name resolution
- Code completion
- Refactoring
- ...

Separation of Concerns in Name Binding

Representation

- Scope Graphs

Declarative Rules

- Scope (& Type) Constraint Rules

Language-Independent Tooling

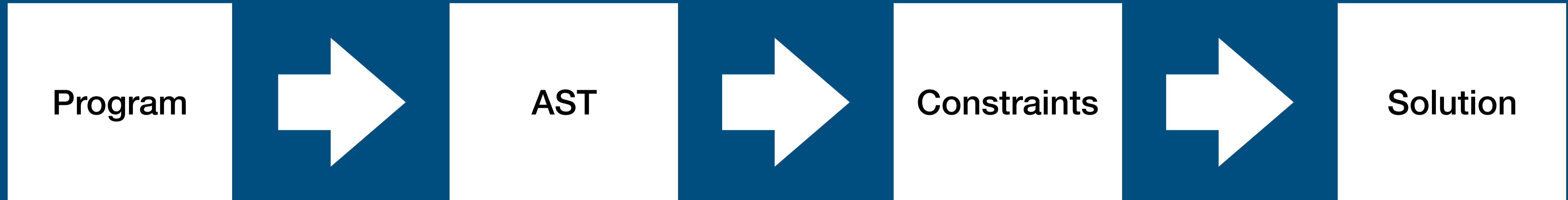
- Name resolution
- Code completion
- Refactoring
- ...

Theory: Constraints

Van Antwerpen, Néron, Tolmach, Visser, Wachsmuth.
A constraint language for static semantic analysis
based on scope graphs. PEPM 2016

NaBL2

Architecture



Parse

**Generate
Constraints**

**Resolve
Constraints**

**Language
Specific**

**Language
Independent**

Scope Graph Constraints

```
new s           // new scope

s1 -L-> s2      // labeled edge from scope s1 to scope s2

N{x} <- s      // x is a declaration in scope s for namespace N

N{x} -> s      // x is a reference in scope s for namespace N

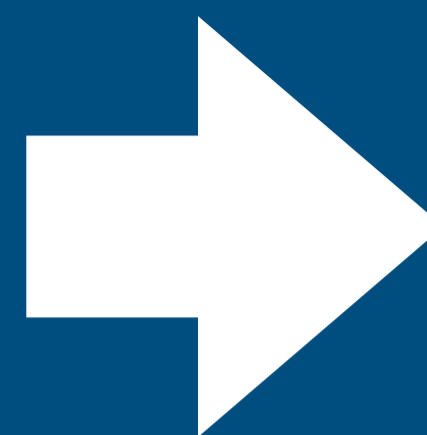
N{x} l-> d      // x resolves to declaration d

[[ e ^ (s) ]]  // constraints for expression e in scope s
```

```

let
  var x : int := x + 1
in
  x + 1
end

```



```

Let(
  [VarDec(
    "x"
    , Tid("int")
    , Plus(Var("x"), Int("1"))
  )]
  , [Plus(Var("x"), Int("1"))]
)

```

```

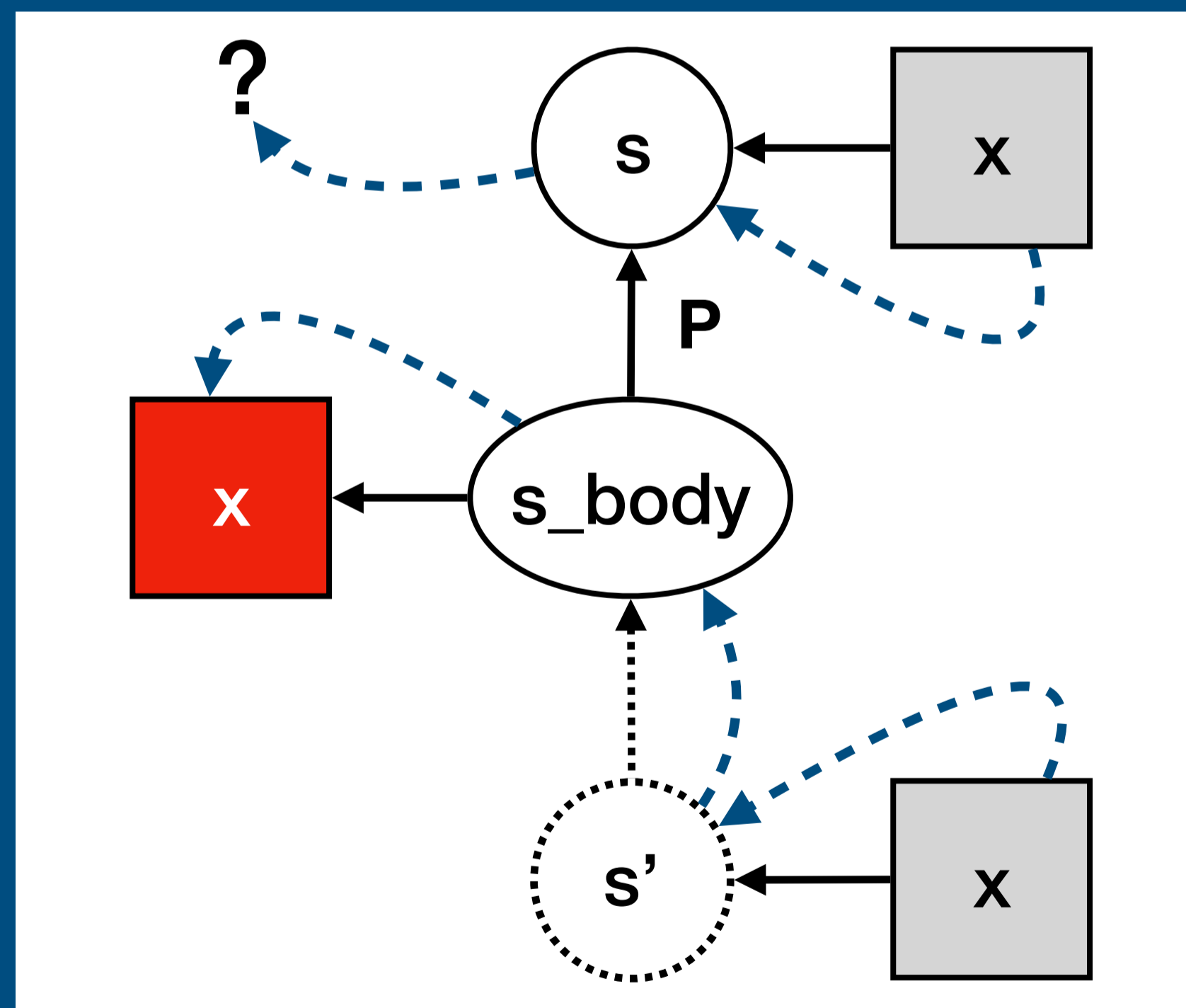
[[ Let([VarDec(x, t, e)], [e_body]) ^ (s) ]] :=
  new s_body,           // new scope
  s_body -P-> s,        // parent edge to enclosing scope
  Var{x} <- s_body,    // x is a declaration in s_body
  [[ e ^ (s) ]],       // init expression
  [[ e_body ^ (s_body) ]]. // body expression

```

```

[[ Var(x) ^ (s') ]] :=
  Var{x} -> s', // x is a reference in s'
  Var{x} l-> d, // check that x resolves to a declaration

```



Type Constraints

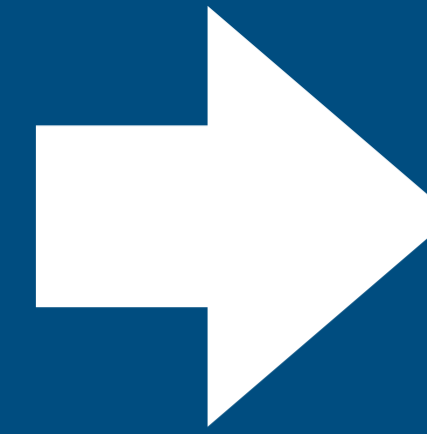
```
d : ty           // declaration has type
t1 == ty2       // type equality
ty1 <! ty2      // declare sub-type
ty1 <? ty2      // query sub-type
ty_gen genOf ty // generalization
ty_gen instOf ty // instantiation
. . .          // extensions
[[ e ^ (s) : ty ]] // type of expression in scope
```



```

let
  var x : int := x + 1
in
  x + 1
end

```



```

Let(
  [VarDec(
    "x"
    , Tid("int")
    , Plus(Var("x"), Int("1"))
  )]
  , [Plus(Var("x"), Int("1"))]
)

```

```

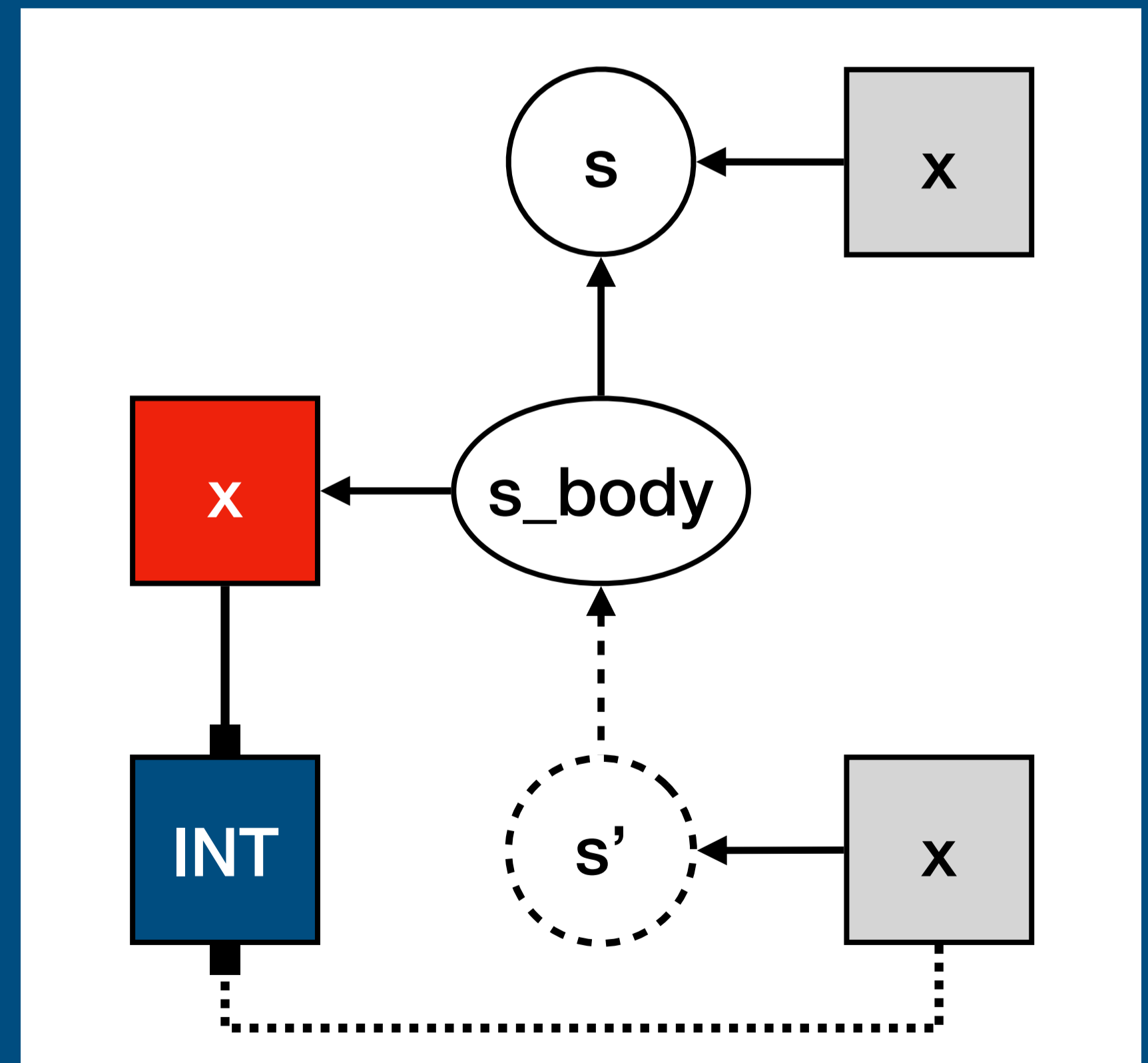
[[ Let([VarDec(x, t, e)], [e_body]) ^ (s) : ty' ]] :=
new s_body,           // new scope
s_body -P-> s,        // parent edge to enclosing scope
Var{x} <- s_body,    // x is a declaration in s_body
Var{x} : ty,         // associate type
[[ t ^ (s) : ty ]],  // type of type
[[ e ^ (s) : ty ]],  // type of expression
[[ e_body ^ (s_body) : ty' ]]. // constraints for body

```

```

[[ Var(x) ^ (s') : ty ]] :=
Var{x} -> s', // x is a reference in s'
Var{x} l-> d, // check that x resolves to a declaration
d : ty.      // type of declaration is type of reference

```



```

let
  type point = {x : int, y : int}
  var origin : point := ...
in origin.x
end

```

```

[[ RecordTy(fields) ^ (s) : ty ]] :=
  ty == RECORD(s_rec),
  new s_rec,
  Map2[[ fields ^ (s_rec, s) ]].

```

```

[[ Field(x, t) ^ (s_rec, s_outer) ]] :=
  Field{x} <- s_rec,
  Field{x} : ty !,
  [[ t ^ (s_outer) : ty ]].

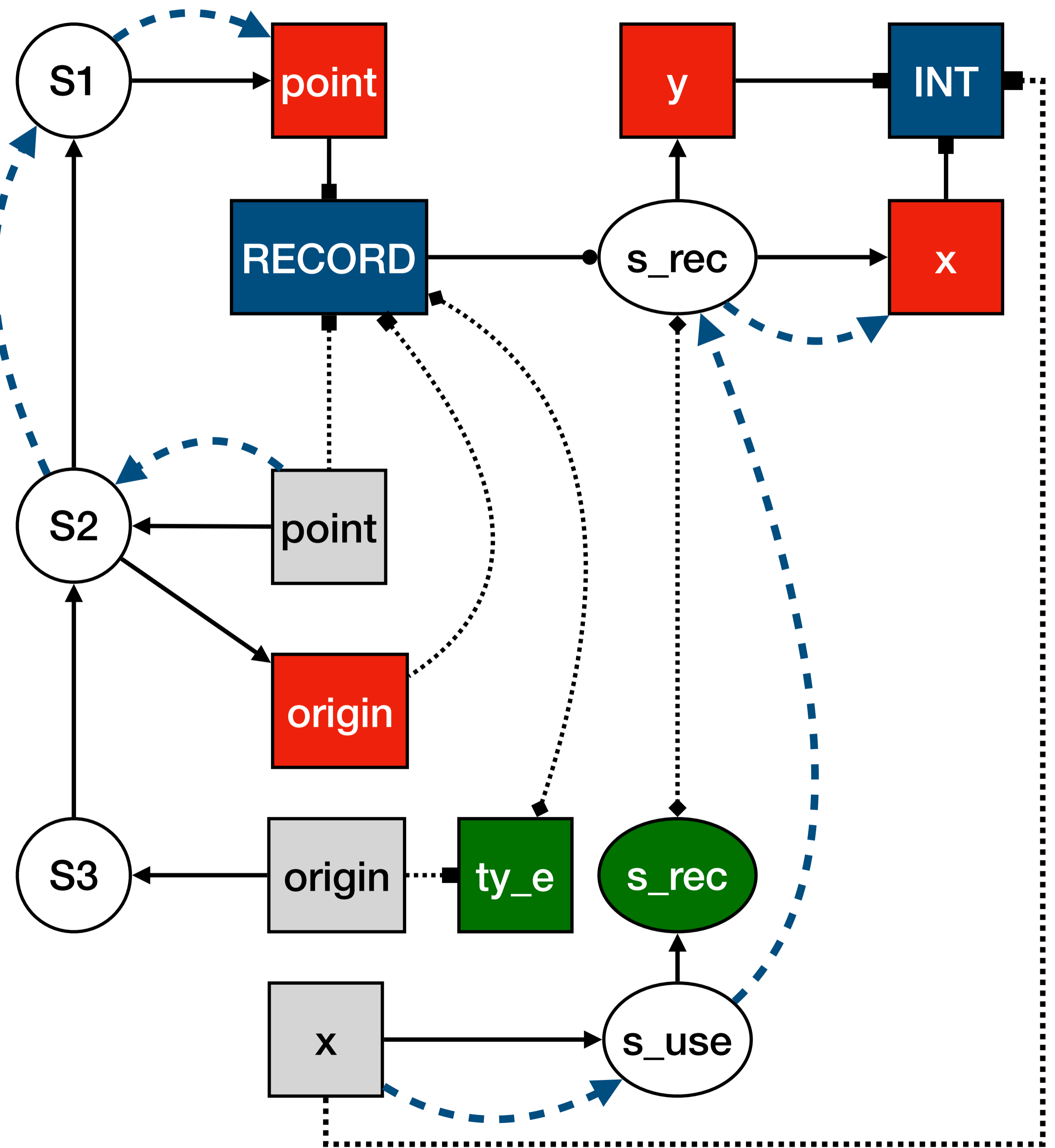
```

```

[[ FieldVar(e, f) ^ (s) : ty ]] :=
  [[ e ^ (s) : ty_e ]],
  new s_use,
  Field{f} -> s_use,
  s_use -I-> s_rec,
  ty_e == RECORD(s_rec),
  Field{f} l-> d,
  d : ty.

```

Type Dependent Name Resolution



Polymorphic Types

```
rules // numbers
```

```
Stat[[ Bind(x, e) ^ (s, s_tmp) ]] :=  
  s_tmp == s_nxt,  
  new s_nxt, s_nxt ----> s,  
  {x} <- s_nxt, {x} : ty_gen,  
  ty_gen genOf ty,  
  [[ e ^ (s) : ty ]].  
  
[[ App(e1, e2) ^ (s) : ty_res ]] :=  
  [[ e1 ^ (s) : ty_fun ]],  
  [[ e2 ^ (s) : ty_arg ]],  
  FunT(ty_arg, ty_res) instOf ty_fun.
```

Name Constraints

```
// Name constraints
e1 subseteq/proj e2 // inclusion
distinct e          // names occur at most once

// Set expressions
∅                  // empty set
R(s)/NS           // references in scope s
D(s)/NS           // declarations in scope s
V(s)/NS           // visible names in scope s

(e1 union e2)
(e1 isect e2)
(e1 minus e2)
```

Name Constraints in Definition of Records (1)

```
rules // record type
```

```
[[ RecordTy(fields) ^ (s) : ty ]] :=  
  new s_rec,  
  ty == RECORD(s_rec),  
  NIL() <! ty,  
  distinct/name D(s_rec)/Field | error $[Duplicate declaration of field [NAME]] @ NAMES,  
  Map2[[ fields ^ (s_rec, s) ]].
```

```
[[ Field(x, t) ^ (s_rec, s_outer) ]] :=  
  Field{x} <- s_rec,  
  Field{x} : ty !,  
  [[ t ^ (s_outer) : ty ]].
```

Name Constraints in Definition of Records (2)

```
rules // record creation
```

```
[[ r@Record(t, inits) ^ (s) : ty ]] :=  
  [[ t ^ (s) : ty ]],  
  ty == RECORD(s_rec) | error $[record type expected],  
  new s_use,  
  s_use -I-> s_rec,  
  D(s_rec)/Field subseteq/name R(s_use)/Field | error $[Field [NAME] not initialized] @r,  
  distinct/name R(s_use)/Field | error $[Duplicate initialization of field [NAME]] @NAMES,  
  Map2[[ inits ^ (s_use, s) ]].
```

```
[[ InitField(x, e) ^ (s_use, s) ]] :=  
  Field{x} -> s_use,  
  Field{x} l-> d,  
  d : ty1,  
  [[ e ^ (s) : ty2 ]],  
  ty2 <? ty1 | error $[type mismatch got [ty2] where [ty1] expected].
```

Tiger Names & Types: Composition

```
module statics/tiger

imports statics/arrays
imports statics/base
imports statics/bindings
imports statics/control-flow
imports statics/functions
imports statics/nabl-lib
imports statics/numbers
imports statics/records
imports statics/strings
imports statics/types
imports statics/variables

rules // top-level module

[[ Mod(e) ^ (s) : ty ]] :=
  [[ e ^ (s) : ty ]].
```

Tiger Names & Types: Composition

```
module statics/functions

imports signatures/Functions-sig
imports statics/nabl-lib
imports statics/base

rules // function declarations

Dec[[ FunDecs(fdecs) ^ (s, s_outer) ]] :=
  Map2[[ fdecs ^ (s, s_outer) ]].

[[ FunDec(f, args, t, e) ^ (s, s_outer) ]] :=
  new s_fun,
  s_fun -P-> s,
  distinct/name D(s_fun) | error $[duplicate argument] @ NAMES,
  MapTs2[[ args ^ (s_fun, s_outer) : tys ]],
  [[ t ^ (s_outer) : ty ]],
  Var{f} <- s,
  Var{f} : FUN(tys, ty) !,
  [[ e ^ (s_fun) : ty_body ]],
  ty == ty_body | error $[return type does not match body] @ t.

[[ FArg(x, t) ^ (s_fun, s_outer) : ty ]] :=
  Var{x} <- s_fun,
  Var{x} : ty !,
  [[ t ^ (s_outer) : ty ]].

rules // function calls

[[ Call(f, exps) ^ (s) : ty ]] :=
  Var{f} -> s,
  Var{f} l-> d | error $[Function [f] not declared],
  d : FUN(tys, ty) | error $[Function expected] ,
  MapSTs[[ exps ^ (s) : tys ]].
```


Tiger Names & Types: Composition

```
module statics/bindings

imports signatures/Bindings-sig
imports statics/nabl-lib
imports statics/base
imports statics/control-flow
imports statics/variables

rules // let

[[ Let(blocks, exps) ^ (s) : ty ]] :=
  new s_body,
  Decs[[ blocks ^ (s, s_body) ]],
  Seq[[ exps ^ (s_body) : ty ]],
  distinct D(s_body).

Decs[[ [] ^ (s_outer, s_body) ]] :=
  s_body -P-> s_outer.

Decs[[ [block] ^ (s_outer, s_body) ]] :=
  s_body -P-> s_outer,
  Dec[[ block ^ (s_body, s_outer) ]].

Decs[[ [block | blocks@[_l_]] ^ (s_outer, s_body) ]] :=
  new s_dec,
  s_dec -P-> s_outer,
  Dec[[ block ^ (s_dec, s_outer) ]],
  Decs[[ blocks ^ (s_dec, s_body) ]],
  distinct/name D(s_dec) | error $[duplicate declaration] @NAMES.
```

```
// Nested scopes: The scope of a variable or parameter includes the
// bodies of any function definitions in that scope. That is, access
// to variables in outer scopes is permitted, as in Pascal and Algol
```

```
/* Local redeclarations: A variable or function declaration may be
hidden by the redeclaration of the same name (as a variable or
function) in a smaller scope; for example, this function prints
"6 7 6 8 6" when applied to 5:
```

```
let
  function f(v : int) =
    let var v := 6
      in print(v);
        let var v := 7 in print(v) end;
          print(v);
            let var v := 8 in print(v) end;
              print(v)
        end
    in f(4)
end
*/
```

Tiger Names & Types: Variables

```
module statics/variables

imports signatures/Variables-sig
imports statics/nabl-lib
imports statics/base

rules // variable declarations

Dec[[ VarDec(x, t, e) ^ (s, s_outer) ]] :=
  [[ t ^ (s_outer) : ty1 ]],
  [[ e ^ (s_outer) : ty2 ]],
  ty2 <? ty1 | error $[type mismatch got [ty2] where [ty1] expected] @ e,
  Var{x} <- s,
  Var{x} : ty1 !.

Dec[[ VarDecNoType(x, e) ^ (s, s_outer) ]] :=
  [[ e ^ (s_outer) : ty ]],
  ty != NIL() | error $[explicit type expected for variable initialized with nil],
  Var{x} <- s,
  Var{x} : ty !.

rules // variable references

[[ Var(x) ^ (s) : ty ]] :=
  Var{x} -> s, // declare x as variable reference
  Var{x} l-> d, // check that x resolves to a declaration
  d : ty.      // type of declaration is type of reference

rules // statements

[[ Assign(e1, e2) ^ (s) : UNIT() ]] :=
  [[ e1 ^ (s) : ty1 ]],
  [[ e2 ^ (s) : ty2 ]],
  ty2 <? ty1 | error $[type mismatch got [ty2] where [ty1] expected] @ e2.
```

Tiger Names & Types: Records (1)

```
module statics/records

imports signatures/Records-sig
imports statics/nabl-lib
imports statics/base

rules // record type

[[ RecordTy(fields) ^ (s) : ty ]] :=
  new s_rec,
  ty == RECORD(s_rec),
  NIL() <! ty,
  distinct/name D(s_rec)/Field | error $[Duplicate declaration of field [NAME]] @ NAMES,
  Map2[[ fields ^ (s_rec, s) ]].

[[ Field(x, t) ^ (s_rec, s_outer) ]] :=
  Field{x} <- s_rec,
  Field{x} : ty !,
  [[ t ^ (s_outer) : ty ]].
```

Tiger Names & Types: Records (2)

```
module statics/records

...

rules // record creation

[[ r@Record(t, inits) ^ (s) : ty ]] :=
  [[ t ^ (s) : ty ]],
  ty == RECORD(s_rec) | error $[record type expected],
  new s_use, s_use -I-> s_rec,
  D(s_rec)/Field subseteq/name R(s_use)/Field | error $[Field [NAME] not initialized] @r,
  distinct/name R(s_use)/Field | error $[Duplicate initialization of field [NAME]] @NAMES,
  Map2[[ inits ^ (s_use, s) ]].

[[ InitField(x, e) ^ (s_use, s) ]] :=
  Field{x} -> s_use,
  Field{x} l-> d,
  d : ty1,
  [[ e ^ (s) : ty2 ]],
  ty2 <? ty1 | error $[type mismatch got [ty2] where [ty1] expected].

rules // record field access

[[ FieldVar(e, f) ^ (s) : ty ]] :=
  [[ e ^ (s) : ty_e ]],
  ty_e == RECORD(s_rec),
  new s_use,
  s_use -I-> s_rec,
  Field{f} -> s_use,
  Field{f} l-> d,
  d : ty.
```

Tiger Names & Types: Records (2)

```
module statics/arrays

imports signatures/Arrays-sig
imports statics/nabl-lib
imports statics/base

rules // array type

[[ ArrayTy(t) ^ (s) : ARRAY(ty, s') ]] :=
  new s', // unique token to distinguish the array type
  [[ t ^ (s) : ty ]].

rules // array creation

[[ Array(t, e1, e2) ^ (s) : ty ]] :=
  [[ t ^ (s) : ty ]],
  ty == ARRAY(ty_elem, s_arr) | error $[array type expected],
  ty_elem2 <? ty_elem | error $[type mismatch [ty_indic] expected] @ e2,
  [[ e1 ^ (s) : INT() ]], // length
  [[ e2 ^ (s) : ty_elem2 ]]. // initial value

rules // array indexing

[[ Subscript(e1, e2) ^ (s) : ty ]] :=
  [[ e1 ^ (s) : ty_arr ]],
  ty_arr == ARRAY(ty, s_arr),
  [[ e2 ^ (s) : INT() ]].
```

Tiger Names & Types: Numbers

```
module statics/numbers

imports signatures/Numbers-sig
imports statics/nabl-lib
imports statics/base

rules // literals

  [[ Int(i) ^ (s) : INT() ]].

rules // operators

  [[ Uminus(e) ^ (s) : INT() ]] :=
    [[ e ^ (s) : INT() ]].

  [[ Divide(e1, e2) ^ (s) : INT() ]] :=
    [[ e1 ^ (s) : INT() ]], [[ e2 ^ (s) : INT() ]].

  [[ Times(e1, e2) ^ (s) : INT() ]] :=
    [[ e1 ^ (s) : INT() ]], [[ e2 ^ (s) : INT() ]].

  [[ Minus(e1, e2) ^ (s) : INT() ]] :=
    [[ e1 ^ (s) : INT() ]], [[ e2 ^ (s) : INT() ]].

  [[ Plus(e1, e2) ^ (s) : INT() ]] :=
    [[ e1 ^ (s) : INT() ]], [[ e2 ^ (s) : INT() ]].

  [[ Eq(e1, e2) ^ (s) : INT() ]] :=
    [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
    ty1 == ty2.
```

```
[[ Neq(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ Gt(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ Lt(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ Geq(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ Leq(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ Or(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.

[[ And(e1, e2) ^ (s) : INT() ]] :=
  [[ e1 ^ (s) : ty1 ]], [[ e2 ^ (s) : ty2 ]],
  ty1 == ty2.
```

Tiger Names & Types: Numbers

```
module statics/control-flow

imports signatures/Control-Flow-sig
imports statics/nabl-lib
imports statics/base

rules // sequence

Seq[[ [] ^ (s) : UNIT() ]].

Seq[[ [e] ^ (s) : ty ]] :=
  [[ e ^ (s) : ty ]].

Seq[[ [ e | es@[_!_] ] ^ (s) : ty ]] :=
  [[ e ^ (s) : ty' ]], Seq[[ es ^ (s) : ty ]].

[[ Seq(es) ^ (s) : ty ]] :=
  Seq[[ es ^ (s) : ty ]].

[[ If(e1, e2, e3) ^ (s) : ty2 ]] :=
  [[ e1 ^ (s) : INT() ]],
  [[ e2 ^ (s) : ty2 ]],
  [[ e3 ^ (s) : ty3 ]],
  ty2 == ty3 | error $[branches should have same type].

[[ IfThen(e1, e2) ^ (s) : UNIT() ]] :=
  [[ e1 ^ (s) : INT() ]],
  [[ e2 ^ (s) : UNIT() ]].

[[ While(e1, e2) ^ (s) : UNIT() ]] :=
  new s', s' -P-> s,
  Loop{""} <- s',
  [[ e1 ^ (s) : INT() ]],
  [[ e2 ^ (s') : UNIT() ]].
```

```
[[ stm@For(Var(x), e1, e2, e3) ^ (s) : UNIT() ]] :=
  new s_for,
  s_for -P-> s,
  Var{x} <- s_for,
  Var{x} : INT(),
  Loop{Break()@stm} <- s_for,
  [[ e1 ^ (s) : INT() ]], // x not bound in loop bounds
  [[ e2 ^ (s) : INT() ]],
  [[ e3 ^ (s_for) : UNIT() ]]. // x bound in body

[[ stm@Break() ^ (s) : UNIT() ]] :=
  Loop{Break()@stm} -> s,
  Loop{Break()@stm} l-> d.
```

Separation of Concerns in Name Binding

Representation

- **Scope Graphs**

Declarative Rules

- **Scope & Type Constraint Rules**

Language-Independent Tooling

- Name resolution
- Code completion
- Refactoring
- ...



**A language
for talking
about name
binding**

NaBL2 in Spoofox Language Workbench

```
workspace - Java - org.metaborg.lang.tiger/trans/statics/records.nabl2 - Eclipse

records.nabl2
20
21 rules // literals
22
23 [[ NilExp() ^ (s) : NIL() ]] := true.
24
25 rules // record creation
26
27 [[ r@Record(t, inits) ^ (s) : ty ]] :=
28   [[ t ^ (s) : ty ]],
29   ty = RECORD(s_rec) | error $[record type expected],
30   new s_use, s_use -I-> s_rec,
31   D(s_rec)/Field subseteq/name R(s_use)/Field | error $[Field [NAME] not initialized] @r,
32   distinct/name R(s_use)/Field | error $[Duplicate initialization of field [NAME]] @NAMES,
33   Map2[[ inits ^ (s_use, s) ]].
34
35 [[ InitField(x, e) ^ (s_use, s) ]] :=
36   Field{x} -> s_use,
37   Field{x} l-> d,
38   d : ty1,
39   [[ e ^ (s) : ty2 ]],
40   ty2 <? ty1 | error $[type mismatch got [ty2] where [ty1] expected].
41
42 rules // record field access
43
44 [[ FieldVar(e, f) ^ (s) : ty ]] :=
45   [[ e ^ (s) : ty_e ]],
46   ty_e = RECORD(s_rec),
47   new s_use, s_use -I-> s_rec,
48   Field{f} -> s_use,
49   Field{f} l-> d,
50   d : ty.

record.tig
1 let
2   type point = {x : int, y : int}
3   var origin : point := point { x = 1, y = 2 }
4   in origin.x
5 end
6
```

Writable Insert

<http://spoofox.org>

Applications

Domain-Specific Languages

- IceDust2 [ECOOP17]
- Green-Marl (Oracle)

Education

- Mini-Java, Tiger, Calc

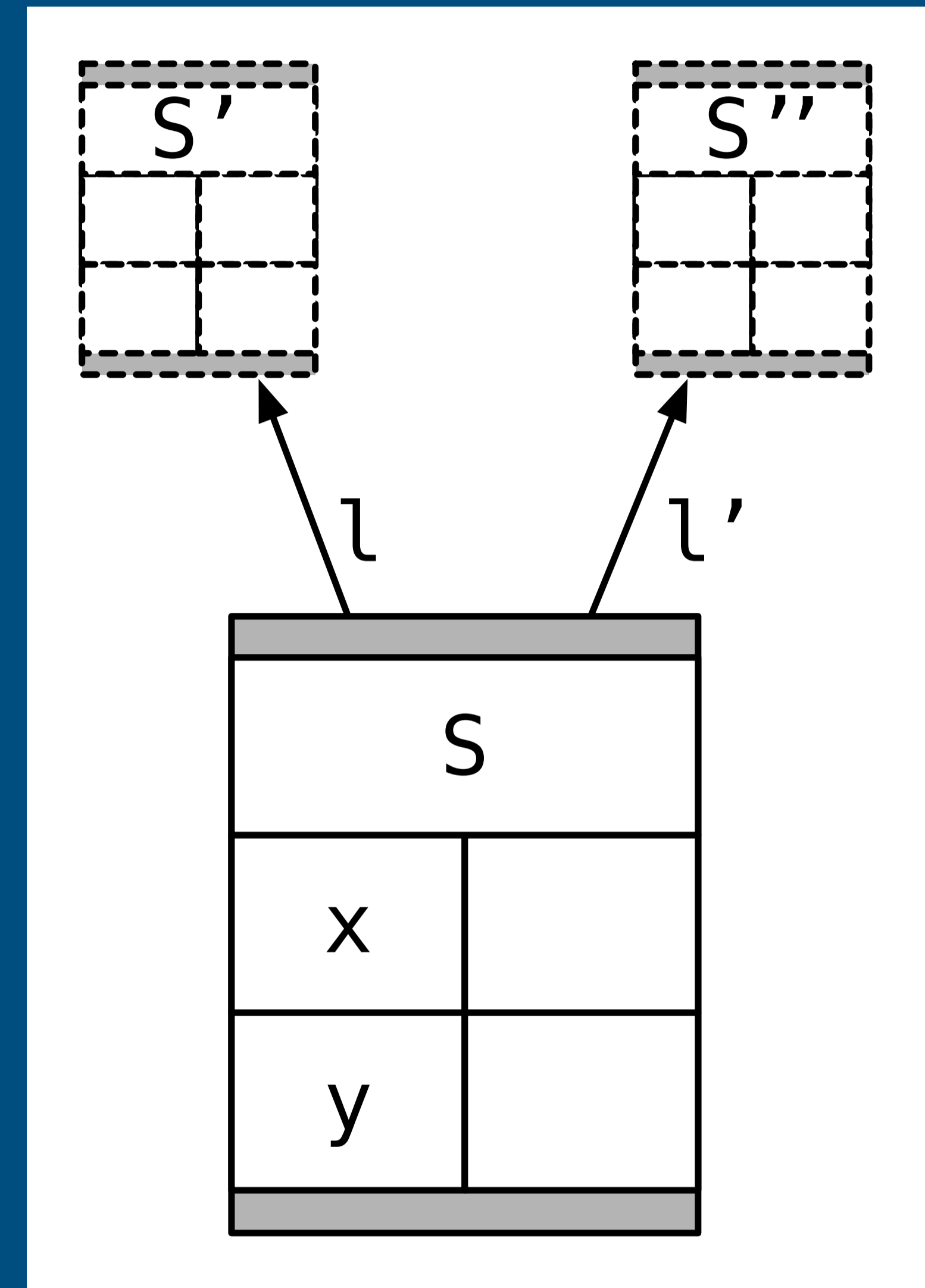
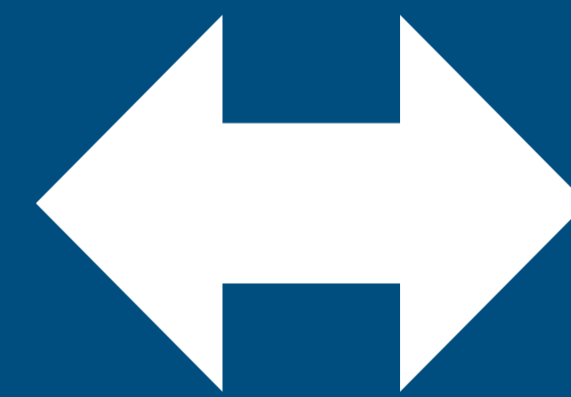
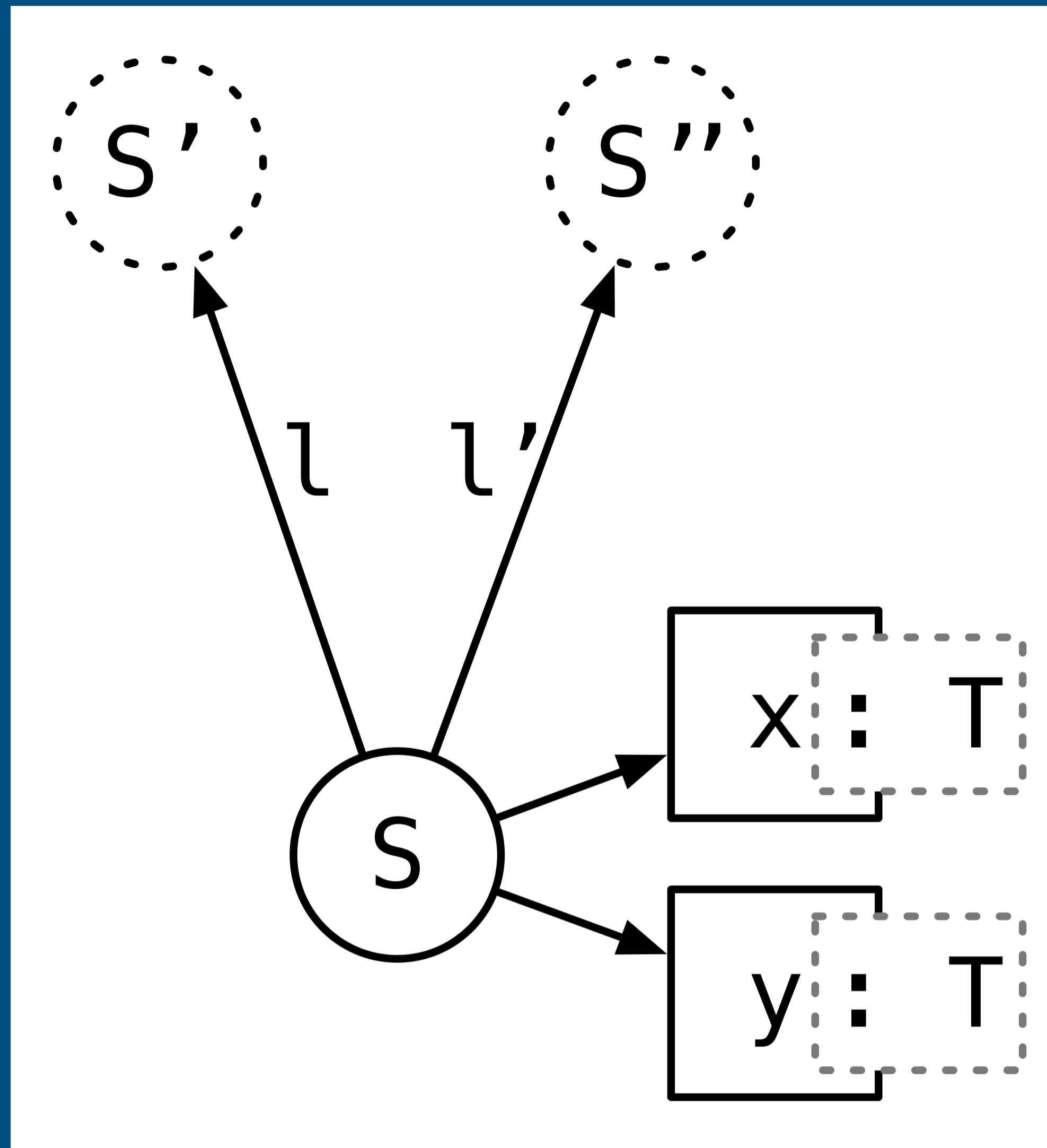
Programming languages

- Pascal, TypeScript, F#, **Go**, Rust
- (student projects in progress)

Bootstrapping language workbench

- NaBL2, ...

Scopes Describe Frames [ECOOP16]



A Uniform Model for Memory Layout
in Dynamic Semantics

Scope Graphs for Name Binding: Status

Theory

- Resolution calculus
- Name binding and type constraints
- Resolution algorithm sound wrt calculus
- Mapping to run-time memory layout

Declarative specification

- NaBL2: generation of name and type constraints

Tooling

- Solver (second version)
- Integrated in Spoofax Language Workbench
 - ▶ editors with name and type checking
 - ▶ navigation

Scope Graphs for Name Binding: Limitations

A domain-specific (= restricted) model

- cannot describe all name resolution algorithms implemented in Turing complete languages

Normative model

- 'this is name binding'

Claim/hypothesis

- Describes all sane models of name binding

Scope Graphs for Name Binding: Future Work

Theory

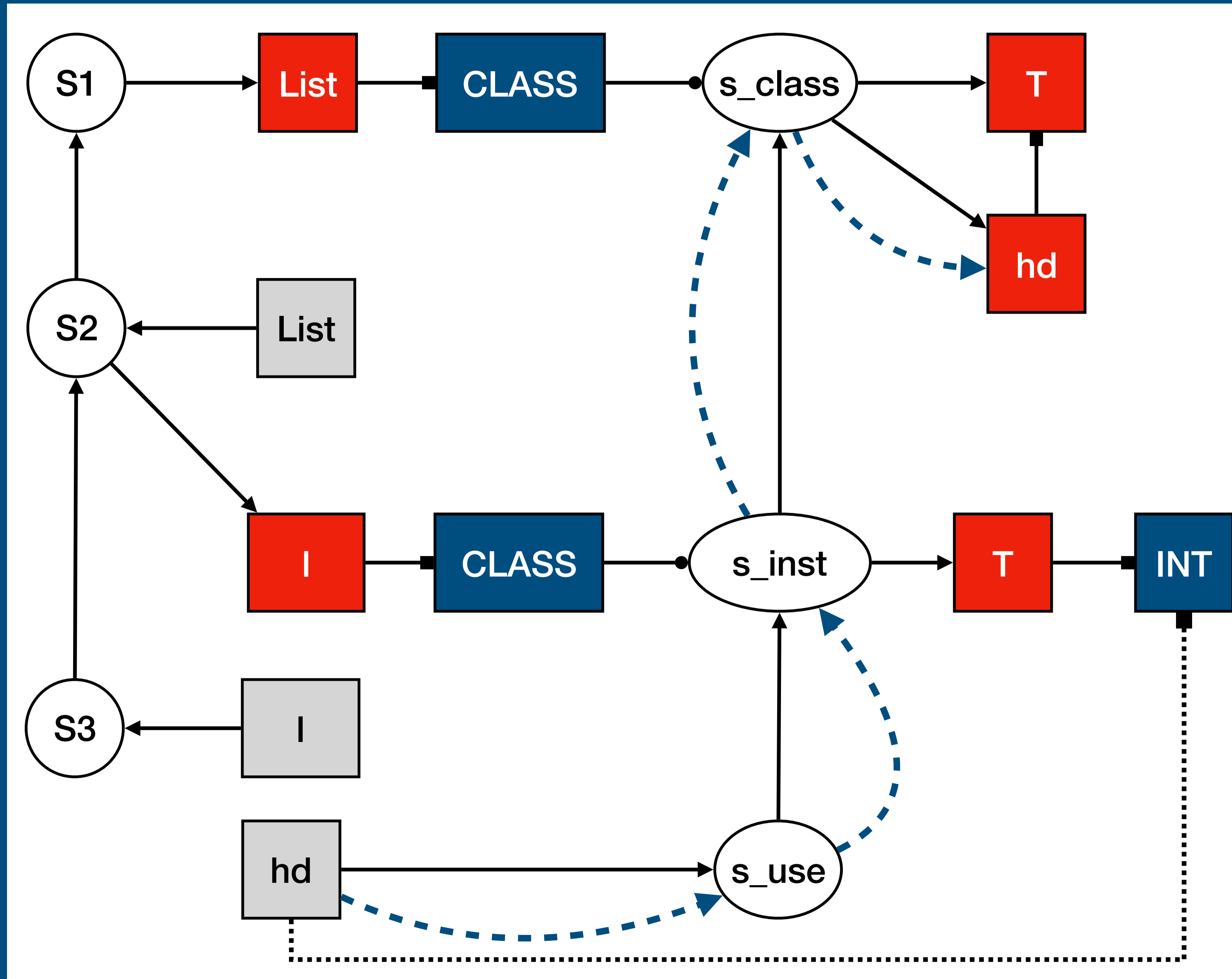
- Scopes = structural types?
 - ▶ operations for scope / type comparison
- Generics
 - ▶ DOT-style?
- Type soundness of interpreters — automatically

Tooling

- Tune name binding language (notation)
- Incremental analysis (in progress)
- Code completion
- Refactoring (renaming)

Generics

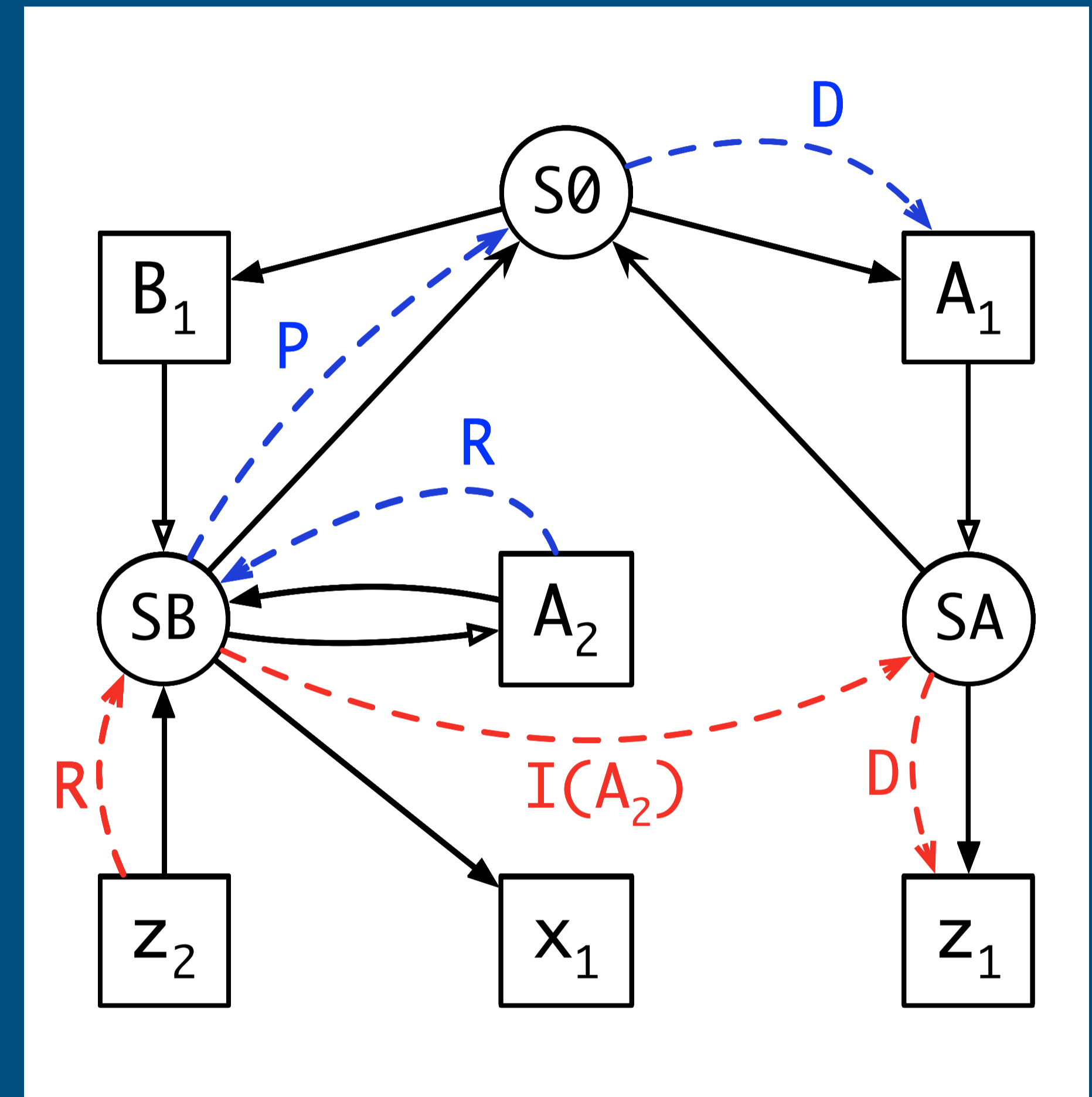
```
class List[T] {  
  def hd : T  
  def tl : List[T]  
}  
val l = new List[Int]  
l.hd
```



Scope Graphs for Name Binding: The Future

A common (cross-language) understanding of name binding

A foundation for formalization and implementation of programming languages



Tiger Syntax

Tiger Syntax: Composition

```
module Tiger

  imports Whitespace
  imports Types
  imports Identifiers
  imports Bindings
  imports Variables
  imports Functions
  imports Numbers
  imports Strings
  imports Records
  imports Arrays
  imports Control-Flow

  context-free start-symbols Module

  context-free syntax

    Module.Mod = Exp

  context-free priorities

    Exp.Or > Exp.Array > Exp.Assign ,

    {Exp.Uminus LValue.FieldVar LValue.Subscript}
    > {left : Exp.Times Exp.Divide}
```

Tiger Syntax: Lexical Syntax

```
module Identifiers
```

```
lexical syntax
```

```
Id = [a-zA-Z] [a-zA-Z0-9\_]*
```

```
lexical restrictions
```

```
Id -/- [a-zA-Z0-9\_]
```

```
lexical syntax
```

```
Id = "nil" {reject}
```

```
Id = "let" {reject}
```

```
Id = ... {reject}
```

```
module Strings
```

```
sorts StrConst
```

```
lexical syntax
```

```
StrConst = "\"" StrChar* "\""
```

```
StrChar = ~["\"\\n]
```

```
StrChar = [\\] [n]
```

```
StrChar = [\\] [t]
```

```
StrChar = [\\] [^] [A-Z]
```

```
StrChar = [\\] [0-9] [0-9] [0-9]
```

```
StrChar = [\\] ["]
```

```
StrChar = [\\] [\\]
```

```
StrChar = [\\] [ \\t\\n]+ [\\]
```

```
context-free syntax // records
```

```
Exp.String = StrConst
```

Tiger Syntax: Whitespace

```
module Whitespace
```

```
lexical syntax
```

```
LAYOUT          = [\ \t\n\r]
CommentChar     = [\*]
LAYOUT          = "/*" InsideComment* "*/"
InsideComment   = ~[\*]
InsideComment   = CommentChar
LAYOUT          = SingleLineComment
SingleLineComment = "//" ~[\n\r]* NewLineEOF
NewLineEOF      = [\n\r]
NewLineEOF      = EOF
EOF             =
```

```
lexical restrictions
```

```
// Ensure greedy matching for lexicals
```

```
CommentChar  -/- [\V]
EOF          -/- ~[]
```

```
context-free restrictions
```

```
// Ensure greedy matching for comments
```

```
LAYOUT? -/- [\ \t\n\r]
LAYOUT? -/- [\V].[\V]
LAYOUT? -/- [\V].[\*]
```

Tiger Syntax: Variables and Functions

```
module Bindings
```

```
imports Control-Flow
imports Identifiers
imports Types
imports Functions
imports Variables
```

```
sorts Declarations
```

```
context-free syntax
```

```
Exp.Let = <
  let
    <{Dec "\n"}*>
  in
    <{Exp ";\n"}*>
  end
>
```

```
Declarations.Declarations = <
  declarations <{Dec "\n"}*>
>
```

```
module Variables
```

```
imports Identifiers
imports Types
```

```
sorts Var
```

```
context-free syntax
```

```
Dec.VarDec = <var <Id> : <Type> := <Exp>>
```

```
Dec.VarDecNoType = <var <Id> := <Exp>>
Var.Var = Id
```

```
LValue = Var
```

```
Exp = LValue
```

```
Exp.Assign = <<LValue> := <Exp>>
```

```
module Functions
```

```
imports Identifiers
imports Types
```

```
context-free syntax
```

```
Dec.FunDecs = <<{FunDec "\n"}+>> {longest-match}
```

```
FunDec.ProcDec = <
  function <Id>( <{FArg ", "*> ) =
    <Exp>
>
```

```
FunDec.FunDec = <
  function <Id>( <{FArg ", "*> ) : <Type> =
    <Exp>
>
```

```
FArg.FArg = <<Id> : <Type>>
```

```
Exp.Call = <<Id>( <{Exp ", "*> )>
```

Tiger Syntax: Numbers

```
module Numbers
```

```
lexical syntax
```

```
IntConst = [0-9]+
```

```
lexical syntax
```

```
RealConst.RealConstNoExp = IntConst "." IntConst
```

```
RealConst.RealConst = IntConst "." IntConst "e" Sign IntConst
```

```
Sign = "+"
```

```
Sign = "-"
```

```
context-free syntax
```

```
Exp.Int = IntConst
```

```
Exp.Uminus = [- [Exp]]
```

```
Exp.Times = [[Exp] * [Exp]] {left}
```

```
Exp.Divide = [[Exp] / [Exp]] {left}
```

```
Exp.Plus = [[Exp] + [Exp]] {left}
```

```
Exp.Minus = [[Exp] - [Exp]] {left}
```

```
Exp.Eq = [[Exp] = [Exp]] {non-assoc}
```

```
Exp.Neq = [[Exp] <> [Exp]] {non-assoc}
```

```
Exp.Gt = [[Exp] > [Exp]] {non-assoc}
```

```
Exp.Lt = [[Exp] < [Exp]] {non-assoc}
```

```
Exp.Geq = [[Exp] >= [Exp]] {non-assoc}
```

```
Exp.Leq = [[Exp] <= [Exp]] {non-assoc}
```

```
Exp.And = [[Exp] & [Exp]] {left}
```

```
Exp.Or = [[Exp] | [Exp]] {left}
```

```
context-free priorities
```

```
{Exp.Uminus}
```

```
> {left :
```

```
Exp.Times
```

```
Exp.Divide}
```

```
> {left :
```

```
Exp.Plus
```

```
Exp.Minus}
```

```
> {non-assoc :
```

```
Exp.Eq
```

```
Exp.Neq
```

```
Exp.Gt
```

```
Exp.Lt
```

```
Exp.Geq
```

```
Exp.Leq}
```

```
> Exp.And
```

```
> Exp.Or
```

Tiger Syntax: Records, Arrays, Types

```
module Records
imports Base
imports Identifiers
imports Types
context-free syntax // records

Type.RecordTy = <
  {
    <{Field ", \n"}*>
  }
>

Field.Field = <<Id> : <TypeId>>

Exp.NilExp = <nil>

Exp.Record = <<TypeId>{ <{InitField ", "}*> }>

InitField.InitField = <<Id> = <Exp>>

LValue.FieldVar = <<LValue>.<Id>>
```

```
module Arrays
imports Types
context-free syntax // arrays

Type.ArrayTy = <array of <TypeId>>

Exp.Array = <<TypeId>[<Exp>] of <Exp>>

LValue.Subscript = <<LValue>[<Index>]>

Index = Exp
```

```
module Types

imports Identifiers
imports Bindings

sorts Type

context-free syntax // type declarations

Dec.TypeDecs = <<{TypeDec "\n"}+>> {longest-match}

TypeDec.TypeDec = <type <Id> = <Type>>

context-free syntax // type expressions

Type = TypeId
TypeId.Tid = Id

sorts Ty
context-free syntax // semantic types

Ty.INT = <INT>
Ty.STRING = <STRING>
Ty.NIL = <NIL>
Ty.UNIT = <UNIT>
Ty.NAME = <NAME <Id>>
Ty.RECORD = <RECORD <Id>>
Ty.ARRAY = <ARRAY <Ty> <Id>>
Ty.FUN = <FUN ( <{Ty ", "}*> ) <Ty>>
```